Rotman

INTRO TO R PROGRAMMING

R Tutorial (RSM358) - Session 3 (Optional Materials)



Binomial Logistic Regression

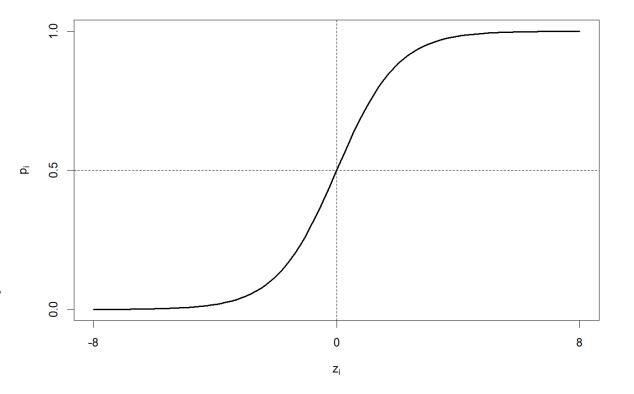
- let Y be a binary outcome variable (i.e., a binary categorical variable)
 - e.g. $Y = \{0, 1\} = \{fail, pass\}, Y = \{0, 1\} = \{down, up\}, etc.$
- Let p = prob(Y = 1); $\frac{p}{1-p}$ is then the odds of being 1
 - The category of Y = 0 is a reference category
 - Reference category is relative as you can instead set p = prob(Y = 0)
- Binary logistic regression models the logit-transformed probability as a linear function of the predictor variables
 - Coefficients $(\beta_0 ... \beta_k)$ are estimated using maximum likelihood method

$$logit(p) = \log\left(\frac{p}{1-p}\right) = \beta_0 + \beta_1 x_1 + \dots + \beta_k x_k.$$

From Log Odds to Probability to Prediction

• Let
$$z_i = logit(p_i) = log(\frac{p_i}{1-p_i}) = \beta_0 + \beta_1 x_{1,i} + \dots + \beta_k x_{k,i}$$
.

- Then, $p_i = \frac{e^{z_i}}{1 + e^{z_i}}$
 - Note $0 < p_i < 1$
- Threshold prob
 - It's a hyper-parameter



Interpret the Coefficients Estimated - 1

- An example: predict (or explain) if a student is in an honors class
 - Outcome variable: hon = {1-Yes, 0-No}. Set No to be the reference category.
 - Predictors are math score, female (1-yes, 0-no), and reading score

$$logit(p) = \beta_0 + \beta_1 math + \beta_2 female + \beta_3 read$$

Ref: https://stats.idre.ucla.edu/other/mult-pkg/faq/general/faq-how-do-i-interpret-odds-ratios-in-logistic-regression/

Interpret the Coefficients Estimated - 2

$$logit(p) = \beta_0 + \beta_1 math + \beta_2 female + \beta_3 read$$

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Ref: https://stats.idre.ucla.edu/other/mult-pkg/faq/general/faq-how-do-i-interpret-odds-ratios-in-logistic-regression/

Logistic Regression in R – Stock Market Ex.

- Import the smarket.csv data
- Prepare the data for logistic regression
 - Convert categorical variables to factor type (Y, and any predictors X)
 - Split data into training and test set
- Perform a logistic regression analysis
 - glm(formula, data, family = binomial) and predict()
 - Construct confusion matrix and calculate accuracy rate