Introduction to Neural Networks and Deep Learning

Brian Keng Chief Data Scientist Rubikloud Technologies brian.keng@rubikloud.com @bjlkeng

Adjunct Professor, Data Science Rotman School of Management, University of Toronto brian.keng@rotman.utoronto.ca

A Brief Overview of Machine Learning



Traditional Programming vs. Machine Learning

Machine Learning: Learning by Example

Write a program with explicit rules:

```
if email contains "V!agr@"
  then mark as spam
else if email contains ...
  then mark as spam
else if email contains ...
  then mark as spam
...
otherwise mark as not-spam
```

Write a program to "learn" from labelled examples by changing itself:

```
try to classify labelled emails
(spam, not-spam)
change self to reduce errors
repeat until satisfied with error
classify unlabeled emails
```

MAN VS. MACHINE

Programming without Humans (ML as Software 2.0)?



Software 2.0, Andrej Karpathy, https://medium.com/@karpathy/software-2-0-a64152b37c35

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Artificial Intelligence

- Artificial Intelligence:
 - Academic discipline that attempts to build machines that mimic human cognitive functions such as "learning" and "problem solving"
- Symbolic AI ("Good Old-Fashioned AI" GOFAI)
 - Logic, Search, Simulation, Expert Systems
- Statistical Learning ("Learning from Data")
 - Machine Learning, Deep Learning, Statistical Inference
- Examples:
 - Forecasting model, Scheduling a timetable, Roomba Vacuum, Computer Chess, Nest Thermostat



What Can Neural Networks Do?

Which one are real vs. Al-generated? (Al Face Generation)



https://arxiv.org/pdf/1812.04948.pdf

Self Driving Cars

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Source: https://www.techiexpert.com/tesla-using-artificial-intelligence-big-data/

Al vs. Doctors



3:20 PM - 15 Nov 2017 from Mountain View, CA

◯ 112 1.4K ♡ 2.4K

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Should radiologists be worried about their jobs? Breaking news: We can now diagnose pneumonia from chest X-rays better than radiologists. stanfordmlgroup.github.io /projects/chexn...

1,436 Retweets 2,387 Likes 🛛 🚳 💽 🥌 🎆 🕦 👘 🔵

AI can detect skin cancer better than doctors now

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PTI | May 29, 2018, 11.58 AM IST



Source:

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Source: https://deepdreamgenerator.com/

Al Art: Deep Dreaming

AI Conversation Bots (Google's Duplex)

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https://www.youtube.com/watch?v=NO0-5MuJvew

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https://youtu.be/PCBTZh41Ris https://arxiv.org/pdf/1808.07371.pdf

AI Making You Dance

Human-Level Language Comprehension

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Seed Human Written Text:

In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.

Machine Generated Text Examples:

The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science.

https://openai.com/blog/better-language-models/

Question and Answer Passage:

The 2008 Summer Olympics torch relay was run from March 24 until August 8, 2008, prior to the 2008 Summer Olympics, with the theme of "one world, one dream". ...

Machine Generated Answers:

- Q: What was the theme? A: "one world, one dream".
- Q: What was the length of the race? A: 137,000 km
- Q: Was it larger than previous ones? A: No
- Q: Where did the race begin? A: Olympia, Greece
- Q: Is there anything notable about that place?
- A: birthplace of Olympic Games

How Did We Get Here?

1 The accelerating pace of change ... 2045 1026 Surpasses brainpower World Human equivalent Agricultural Industrial Light-Moon 8,000 120 years + 90 years -Wide 22 years 9 years genome to that of Revolution years Revolution bulb landing Web sequenced all human brains combined 102 Surpasses brainpower 3 ... will lead to the 2 ... and exponential growth of human in 2023 in computing power ... Singularity Computer technology, shown here climbing dramatically 1015 by powers of 10, is now progressing more each Apple II hour than it did in its Nvidia Tesla At a price of \$1,298, entire first 90 years GPU & PC the compact machine was one of Mac Pro UNIVAC I Surpasses the first massively 10,000,000,000 The first commerbrainpower of popular personal cially marketed mouse in 2015 computers computer, used to Dimension 8400 Colossus tabulate the U.S. COMPUTER RANKINGS The electronic Census, occupied By calculations per second per \$1,000 computer, with 943 cu. ft. II PC Pentium PC IBM P 1,500 vacuum 100,000 tubes, helped the Compag Deskpro 386 British crack German Analytical engine codes during WW II DEC Never fully built. 1130 PDP-4 Charles Babbage's . Intellec-8 nvention was Whichaind DEC Power Mac G4 designed to solve PDP-10 IBM 1620 The first personal computational and logical problems ENIAC computer to deliver . Datamatic more than 1 billion FDMAC IRM 1000 floating-point Zuse 3 SSEC Zuse 2 IBM Tabulator operations per . National second Tabulato Ellis 3000 0.00001 ELECTROMECHANICAL INTEGRATED CIRCUITS 1900 1960 1980 1920 1940 2000 2011 2020 2045

Massive Growth in Computing Power...

Source: http://content.time.com/time/interactive/0%2C31813%2C2048601%2C00.html

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And Massive Growth in Data...

Data Growth



Problem - Traditional and Legacy Storage Designed for Transactional, Not Unstructured Data

https://www.dubber.net/unlocking-unstructured-data-voice-processing-power-zoe/

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And Some Research...



Made by Favio Vázquez

https://towardsdatascience.com/a-weird-introduction-to-deep-learning-7828803693b0

Why Are Neural Networks So Good?

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Manual Feature Engineering

Original	Gaussian Blur	Sharpen	Edge Detection
$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	$\frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$	$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$	$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$

Source: https://santexgroup.com/blog/tag/tensor-flow/

Automatic Feature "Learning"

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Source: https://stats.stackexchange.com/questions/146413/why-convolutional-neural-networks-belong-to-deep-learning

Automatic Feature "Learning"

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Source: https://www.kdnuggets.com/2016/11/intuitive-explanation-convolutional-neural-networks.html/3

Neural Networks are Scalable

IVIOGEI	Number of Parameters
Linear Regression	< 100
LeNet (1998)	60K
AlexNet (2012)	60M
VGG-16 (2014)	138M
Inception-v3 (2015)	23M
ResNet-152 (2015)	60M



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Source: https://www.kdnuggets.com/2016/11/intuitive-explanation-convolutional-neural-networks.html/3 "AN ANALYSIS OF DEEP NEURAL NETWORK MODELS FOR PRACTICAL APPLICATIONS", https://arxiv.org/pdf/1605.07678.pdf

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Neural Networks as Function Approximators

Functions and Machine Learning

A function f maps each element in the *domain* (X) to a single element in the **range** (Y). Most functions we see are real-valued functions, e.g.:

- $f(x) = 2x^2 + 3$
- $g(x_0, x_1) = e^{\alpha x_0 + \beta x_1 + C}$

Data = (X, Y) can be thought of as^{*}:

- Inputs X (i.e. features, regressors, covariates etc.)
- Outputs Y (i.e. observations, response variables, labels etc.)

One useful way to think about machine learning is as *function approximation*:

• Finding a function that "fits" the data according to some mathematical objective function

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Approximating the data using a line of best fit

^{*} This is only *one* (of many) ways to view ML; there are many lenses to understand it (e.g. probabilistically, algorithmically, optimization etc.)

What Makes a Good Function Approximator: Linear?

 $\longrightarrow y = f(x) = \beta_1 x + \beta_0$



Response

Variable

- 1 feature (aka covariate, independent variable, predictor, regressor)
- 1 *response* variable (aka *output, dependent variable*)
- Linear models are rigid (not much flexibility)



Parameters

Features

More Complex Linear Function?

$$y = f(x) = \beta_3 x^3 + \beta_2 x^2 + \beta_1 x + \beta_0$$

- 4 parameters (β_3 , β_2 , β_1 , β_0)
- 3 features (x^3, x^2, x) where each feature is a function of our original covariate
- Need to use intuition to come up with right features (transformations of raw data observations)



How about a Neural Network? (Definitions)

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Define a non-linear ("activation") function:

 $ReLU(\mathbf{x}) \coloneqq \max(0, \mathbf{x})$ (element-wise)

Define a "hidden layer" function:

$$H_{n,d}(\boldsymbol{x}) = ReLU(\boldsymbol{W}\boldsymbol{x} + \boldsymbol{b}) = ReLU(\begin{bmatrix} w_{11} & \cdots & w_{1d} \\ \vdots & \ddots & \vdots \\ w_{n1} & \cdots & w_{nd} \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix} + \begin{bmatrix} b_1 \\ \vdots \\ b_n \end{bmatrix}$$

How about a Neural Network?

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5 hidden layer neural network with 500 hidden units:

$$y = f(x) = (H_{1,500}) \circ (H_{500,500}) \circ (H_{500,500}) \circ (H_{500,500}) \circ (H_{500,500}) \circ (H_{500,1})(x)$$
$$= H_{1,500} \left(H_{500,500} \left(H_{500,500} \left(H_{500,500} \left(H_{500,500} \left(H_{500,1}(x) \right) \right) \right) \right) \right)$$

- 1M+ parameters (each w_{ij} 's in each W matrix is a parameter)
- 1 features (x)
- No need for any feature engineering



Basics of Feed Forward Neural Networks

(aka Multi-Layer Perceptrons, Feed Forward Neural Networks, Deep Feedforward Networks, Dense Neural Networks, Fully Connected Neural Networks)

Demo: Neural Network Playground

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https://playground.tensorflow.org/

The Anatomy of a Perceptron (aka neurons)

- Inputs (x_i): input features (or outputs from previous layers)
- Weights (*w_j*): Learnable real-valued parameters (this is akin to learning the "slope" and "intercept" of a line)
- Sum (Σ): Summation of product of weights and inputs
- Activation Function (*σ*): Non-linear function mapping z to a (usually monotonic and continuous)
- **Bias** (**b**): "Intercept" for the perceptron (can be implemented by making one input constant)



$$f(\mathbf{x}) = \sigma(\sum_{i=1}^{n} w_i x_i + b) = \sigma\left(\begin{bmatrix} w_1 & \cdots & w_n \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix} + b\right) = \sigma(\mathbf{W}^T \mathbf{x} + b)$$

What Makes a Perceptron Special?



- Non-linear function allows perceptron to learn "interesting" functions
- The more perceptrons you have, the more "interesting" functions you can learn

A Very Simple Neural Network

- Input Layer: represents input features
- Hidden Layer: represents perceptrons in any non-input/non-output layers
- **Output Layer**: represents perceptrons used to generate final output(s) (for now just the identify function)

Name	Value
Inputs	2
Parameters	(1.2+1) + (1.1+1) = 3+2 = 5
Hidden Layers	1
Output Layers	1
Depth	2
Width	[2, 1, 1]

Input Hidden Output

$$f(\mathbf{x}) = y_1 = Id\left(w_{2,1,1} \cdot \sigma\left(\left[w_{1,1,1} \ w_{1,1,2}\right] \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + b_{1,1}\right) + b_{2,1}\right)$$
$$= \mathbf{w}_2 \cdot \sigma\left(\mathbf{w}_1 \mathbf{x} + b_{1,1}\right) + b_{2,1}$$

Adding More Perceptrons

$$\begin{aligned} f(\mathbf{x}) &= \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} \\ &= Id \left(\begin{bmatrix} w_{2,1,1} & w_{2,2,1} & w_{2,3,1} \\ w_{2,1,2} & w_{2,2,2} & w_{2,3,2} \end{bmatrix} \cdot \sigma \left(\begin{bmatrix} w_{1,1,1} & w_{1,2,1} \\ w_{1,1,2} & w_{1,2,2} \\ w_{1,1,3} & w_{1,2,3} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} b_{1,1} \\ b_{1,2} \\ b_{1,3} \end{bmatrix} \right) + \begin{bmatrix} b_{2,1} \\ b_{2,2} \end{bmatrix} \right) \\ &= W_2 \cdot \sigma (W_1 \mathbf{x} + \mathbf{b}_1) + \mathbf{b}_2 \end{aligned}$$

Hidden

Name	Value
Inputs	2
Parameters	(3·2+3) + (2·3+2) = 17
Hidden Layers	1
Output Layers	1
Depth	2
Width	[2, 3, 2]



Adding More Layers...

$$f(\mathbf{x}) = \begin{bmatrix} y_1 \\ y_2 \end{bmatrix}$$

= $W_4 \cdot \sigma(W_3 \cdot \sigma(W_2 \cdot \sigma(W_1 \mathbf{x} + \mathbf{b}_1) + \mathbf{b}_2) + \mathbf{b}_3) + \mathbf{b}_4$

Name	Value
Inputs	3
Parameters	(4·3+4) + (4·4+4) + (4·4+4) + (3·4+3) = 71
Hidden Layers	3
Output Layers	1
Depth	4
Width	[3, 4, 4, 4, 3]



A "Deep" Neural Network...

Name	Value
Inputs	5
Parameters	(10·5+10) + 9·(10·10+10) + (5·10+5) = 1105
Hidden Layers	10
Output Layers	1
Depth	11
Width	[5, 10, 10, 10, 10, 10, 10, 10, 10, 10, 10, 5]



"Deep" = Many of Layers (definition of deep changes as deeper networks are built)

How Do We Define the Output Perceptrons?

- Output neurons model the "y" values (or labels)
- Activation function should match your response variable
- Considerations:
 - Regression vs Classification problem
 - Range of output variable
 - Loss function (see this later)
 - Discrete vs. Continuous
- We'll look at 4 common activation functions for output units:
 - Identity
 - ReLU
 - Sigmoid
 - Softmax



Output Units (Linear, Positive Real-Valued)

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Linear Output (Identity Activation Function)

- Real-valued output $(y \in [-\infty, \infty])$
- Appropriate for general regression problems

$$y = W^T h + b$$



Positive-Valued Output

- Real-valued output $(y \in [0, \infty])$
- Appropriate for general regression problems

$$y = ReLU(W^T h + b)$$

Output Units (Binary, Categorical)



Binary Probability Output

- Real-valued output $(y \in [0,1])$
- Appropriate for binary classification problems
- Output variable is probability of "1" label

$$y = sigmoid(W^T h + b)$$



Softmax (Multinomial/Categorical Probability) Output

- Categorical Probability $(y_i \in [0,1], \sum_i y_i = 1)$
- Appropriate when output labels are categorical labels (e.g. Red, Green Blue, Yellow)
- N output variables corresponding to a probability distribution across N categories

$$\boldsymbol{z} = \boldsymbol{W}^T \boldsymbol{h} + \boldsymbol{b}$$
 $y_i = \frac{e^{z_i}}{\sum_j e^{z_j}}$

Example: A Neural Network for the XOR Function

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- XOR is a basic logic binary operation
- XOR is not *linearly separable* (can't draw a line to separate 0/1 classes)

Question:

• XOR is only defined on inputs with {0,1}, what should our network return for other inputs (e.g. $x_1 = 0.5, x_2 = 0.5$)?



XOR Function

Example: Define Our Neural Network

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Write out as equations (using the RELU activation and linear output):

$$f(\mathbf{x}; \mathbf{W}, \mathbf{c}, \mathbf{w}, b) = \mathbf{w}^T \max(0, \mathbf{W}^T \mathbf{x} + \mathbf{c}) + b$$

= $\begin{bmatrix} w_{2,1} & w_{2,2} \end{bmatrix} \max(0, \begin{bmatrix} w_{1,1,1} & w_{1,2,1} \\ w_{1,1,2} & w_{1,2,2} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} c_0 \\ c_1 \end{bmatrix} + b$

Given training input data: $\boldsymbol{X} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix}, \quad \boldsymbol{y} = \begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}$

Find values of **W**, **c**, **w**, **b** that minimize error (in this case mean squared error):

$$\sum_{x_i, y_i \in (X, y)} (y_i - f(x_i; W, c, w, b)^2$$



Example: Solving our Network

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Here's a solution that solves this problem:

$$W = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}, \qquad \mathbf{c} = \begin{bmatrix} 0 \\ -1 \end{bmatrix}, \qquad \mathbf{w} = \begin{bmatrix} 1 \\ -2 \end{bmatrix}, \qquad b = 0$$

Let's see how these weights (or parameters) solve the XOR problem by doing a "forward pass" of a neural network:

$$f(\mathbf{x}; \mathbf{W}, \mathbf{c}, \mathbf{w}, b) = \mathbf{w}^T \max(0, \mathbf{W}^T \mathbf{x} + \mathbf{c}) + b$$

First, compute the first weight matrix with our features $\boldsymbol{W}^T \boldsymbol{x}$ (we'll compute all four data points at once):

$$\boldsymbol{X}\boldsymbol{W} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 1 & 1 \\ 1 & 1 \\ 2 & 2 \end{bmatrix}$$

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Example: Solving our Network (continued)

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Next, add our constant bias $W^T x + c$: $\begin{bmatrix} 0 & 0 \\ 1 & 1 \\ 1 & 1 \\ 2 & 2 \end{bmatrix} + \begin{bmatrix} 0 & -1 \\ 0 & -1 \\ 0 & -1 \\ 0 & -1 \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \\ 1 & 0 \\ 2 & 1 \end{bmatrix}$

Next, add apply the activation function (i.e. ReLU)
$$\max(0, W^T x + c)$$
: $\max(0, \begin{bmatrix} 0 & -1 \\ 1 & 0 \\ 1 & 0 \\ 2 & 1 \end{bmatrix}) = \begin{bmatrix} 0 & 0 \\ 1 & 0 \\ 1 & 0 \\ 2 & 1 \end{bmatrix}$

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Finally, apply weights from the last layer
$$\boldsymbol{w}^T \max(0, \boldsymbol{W}^T \boldsymbol{x} + \boldsymbol{c}) + b$$
:
$$\begin{bmatrix} 0 & 0 \\ 1 & 0 \\ 1 & 0 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} + \boldsymbol{0} = \begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}$$

Example: Illustration of Non-Linear Hidden Layers







Much More to Neural Networks...

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Fundamentals Concepts of Neural Networks

- Training Deep Neural Networks
 - Computation graphs and computing gradients
 - Optimization through Stochastic Gradient Descent
- Neural Network Architectures
 - Width, depth
 - Types of layers
 - Connectivity
 - Activation functions
 - Loss functions
- Tuning Deep Neural Networks
 - Overfitting vs. Underfitting
 - Regularization
 - Learning rate
 - Hyper-parameters tuning



Summary of Neural Networks

- Neural networks are *big* function approximators with 100Ms of parameters
 - Allows them to approximate *very* complicated functions
- Feedforward Neural Networks are composed of simple functions called **perceptrons**:
 - Compute a linear combination of inputs and parameters with a non-linear activation function
- "Deep" neural networks (i.e. deep learning) are just neural networks with many layers
- Neural networks have only recently (~10 years) become very useful because of exponential growth in computing power (and correspondingly data)



"Deep" Neural Network

Deep Learning and Beyond

Convolutional Neural Networks

- · CNNs are composed on multiple successive layers of convolutional layers and fully-connected layers
 - · Backbone of modern image processing ML to produce state-of-the-art results
 - · Convolutional layers are used to extract features from the original input size
 - Final few layers are usually FC layers to produce output (e.g. image classification)
 - Non-linear activation functions are implicit in diagrams



Source: https://en.wikipedia.org/wiki/Convolutional_neural_network#/media/File:Typical_cnn.png

"Deep" Neural Networks ("ResNet")

- He, Zhang, Ren, Sun, "Deep Residual Learning for Image Recognition", 2015
 - Achieved 4.49% top-5 error rate; 60M parameters
 - https://arxiv.org/abs/1512.00567
- Introduced concept of "Residual Learning":
 - Try to learn H(x) x (left branch) instead of directly learning H(x)
 - · Adds "shortcut" connections that are added back to the CNN operations
 - Residual blocks enable "deep" networks up to 152 layers



Two Different Residual Blocks

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Representation Learning

- **Representation Learning** (or feature learning) is a broad set of techniques to automatically discover the representation needed for a specific task from raw data.
 - **Supervised techniques**: Use labelled data to infer the right feature representation (e.g. deep nets)
 - Unsupervised techniques: Use unlabeled data to infer (usually compact) representations of the data
- Examples:
 - Images & CNNs: Each successive convolutional layer is a "feature map", forming a hierarchy of features
 - Word embeddings (shown later): Representing words as a highdimensional continuous real vector
 - Dimensionality Reduction e.g. Principal Component Analysis (PCA)



Source: https://cse.iitk.ac.in/users/piyush/courses/ml_autumn16/771A_lec23_slides.pdf

Transfer Learning

- Transfer Learning: transfer "knowledge" learned in one or more ML source tasks to improve performance on a related target task
 - Labelling data is expensive, thus most data is unlabeled
 - Utilize the large base of labelled data to improve performance on tasks with small amounts of data
- Example:
 - · Task: Classifying male/female dolphins images
 - · Not much labelled data, expensive to obtain
 - Pre-train a deep net network (e.g. ResNet-152) on ImageNet (14M labelled images)
 - Use the pre-trained network to generate features from existing dolphin images
 - · Train a new classifier using these new features

https://www.datasciencecentral.com/profiles/blogs/transfer-learning-deep-learning-for-everyone

RSM8431 Neural Networks II

Transfer learning: idea



Modeling Sequence Data with RNNs

- Recurrent Neural Networks (RNN) are a family of neural networks for processing sequential data
- Key RNN ideas:
 - Neural networks have a time varying state (h_t)
 - Utilize the same function (aka "RNN cell") f(...) to map h_t, x_t to h_{t+1}
 - Computational graph is *unfolded* through time to perform stochastic gradient descent
- Applications:
 - Time-series problems (e.g. stock prices, sales forecasting)
 - Video / audio / text prediction tasks (e.g. image caption generation, machine translation etc.)

Image Captioning Architecture



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Source: https://www.analyticsvidhya.com/blog/2018/04/solving-an-image-captioning-task-using-deep-learning/

Generative Adversarial Networks (GAN)

- GANs are composed of two deep nets:
 - *Generator* network which generates fake samples of the data conditioned on latent space (random noise)
 - **Discriminator** network which attempts to tell the real samples from the fake (generator) samples
- The generator and discriminator play an **adversarial game** where:
 - Generator tries to fool the discriminator; and
 - · Discriminator tries to guess that the data is fake
- The generator and discriminator networks alternate updating via SGD in attempt to "win" via a two player minimax game
- Applications:
 - · Image / video / audio synthesis
 - Text generation



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GAN Architecture

$$V(D,G) = E_{x \sim p_{data}(x)}[\log D(x)] +$$
$$\min_{G} \max_{D} E_{z \sim p_{Z}(z)}[\log (1 - D(G(Z)))]$$

Source: https://stats.stackexchange.com/questions/277756/some-general-questions-on-generative-adversarial-networks

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